Eleventh LACCEI Latin American and Caribbean Conference for Engineering and Technology (LACCEI'2013) "Innovation in Engineering, Technology and Education for Competitiveness and Prosperity" August 14 - 16, 2013 Cancun, Mexico.

Modeling the logistic chain of lettuce in Panama

Humberto Ramón Álvarez Alvarado

Universidad Tecnológica de Panamá, Panamá, Panamá, Panamá, humberto.alvarez@utp.ac.pa

Andrés Orozco

Universidad Marítima Internacional de Panamá, Panamá, Panamá, Panamá, aorozco@umip.ac.pa

ABSTRACT

Despite being recognized as an international logistics center, Panama has no records of deep analysis of their internal logistics chains that allow you to understand their behavior. This paper presents the preliminary results of a project funded by the National Secretariat for Science, Technology and Innovation of the Republic of Panama, which aims to model and analyze the supply chain of agricultural products, specifically lettuce, in the country. The model presents the behavior of an agricultural product logistics chain, considering aspects such as costs of shipment and the availability of vehicles for transportation.

Keywords: Agricultural logistic chains, mathematical optimization.

RESUMEN

A pesar de ser reconocida como un centro logístico internacional, Panamá no tiene registros de análisis profundos de sus cadenas logísticas internas que permitan entender su comportamiento. Este trabajo presenta los resultados preliminares de un proyecto financiado por la Secretaría Nacional de Ciencia, Tecnología e Innovación de la República de Panamá, cuyo objetivo es modelar y analizar la cadena de suministros de productos agrícolas, específicamente lechuga, en el país. El modelo presenta el comportamiento de la cadena logística de un producto agrícola, considerando aspectos tales como costos de envío y la disponibilidad de vehículos para su transporte.

Palabras claves: Cadenas logísticas agropecuarias, optimización matemática.

1. INTRODUCTION

Panama has been considered a logistics center point for the American Continent. According to the Panamanian Government Five Year Strategic Plan, it has been considered to create in the country a world class center of logistics added value services, luxury tourism, high value agriculture and thus enhance its privilege geographical position and the comparative advantages, decreasing the unemployment rate and increasing the economic growth between 6% and 9% annual, also to generate approximately 500,000 new jobs.

The objective of this paper is to develop a mathematical model that depicts both the behavior of the agricultural supply chain and to analyze the transportation equipment used in the logistic chain in order to obtain an optimal transportation policy of agricultural products through the country. This optimization model is one of the outcomes of an oingoing project funded by the National Secretariat of Science, Technology and Innovation of Panama entitled "Designing a logistic platform through the optimization of distribution networks for the agricultural sector." The project is aimed to study the distribution network of agricultural products and propose a decision making model for optimal locations of modal interchange facilities and logistics platforms. The rest of the document will present a description of the current situation, a brief literature review of work done in this area, the methodology used and a first approach to the model and its solution.

2. PROBLEM STATEMENT

According to the 2012 Key Performance Indicators of the Republic of Panama, published by the General Ccounting Office, although agriculture and other related activities are the main sources of employment in the rural areas, providing the 19% of total employment nationwide the Agricultural Gross Domestic Product (AGDP - 2011) it represents just 3% of total Gross Domestic Product (GDP). Thus, lack attention has been provided to the analysis, modeling and optimization of the internal agricultural supply chain.

The Province of Chiriquí located at the west side of the country (see map in figure 1) provides almost 80% of the vegetables consumed in Panama, thus being the main supplier node in the food distribution network of the country. On the other hand, the Province of Panama at about 500 kilometers east of Chiriquí is the largest market with almost 50% of the population, hence an optimal distribution networks system is required throughout the country to serve not only the Province of Panama, but also the rest of the provinces in an efficiently way.

To find the contextual description for the current situation, preliminary data from the different distribution points was gathered. In addition, an exploratory research was conducted in several locations around the country in order to know the situation and understand the behavior of the distribution of products at these points. The information from these sources was collected through interviews and questionnaires applied to a group of stakeholders that were selected more by convenience than by random selection. Data such as transportation costs, operation costs, vehicles availability, production capacities, market demand, warehouses and distribution capacities were gathered.

In addition, data from the National Secretary of the Cold Chain and the Agro-Marketing Institute allowed the researchers to have production data. Furthermore, the data collected from these organizations helped the researchers to compare this information with the one collected from the suppliers and consumers. At this point, the information is being carefully analyzed since there are significant differences between the information collected.

With the information provided, a map of the distribution network was developed. This map is shown in figure 1. As seen, two production areas were located. As seen, the supply chain has a longitudinal configuration, with two main production points and several transhipment centers. The main issue of the chain is that over 50% of the products have to be delivered to Panama City, while the rest of the products are delivered to the rest of the central provinces.

Products are transported from these areas to different distribution points. These points are David, the largest city of Chiriquí, which distributes products to the rest of the province. Also, products are sent to Santiago, in the Province of Veraguas, which distributes products to the province, and also sends products to other areas of in the middle of the country that serve also as intermediate distribution centers. Finally, they send most of their production capacity to the Central Supply Market, which is the main distribution point in Panama City. This center supplies products to the west, east, north and central areas of the Province of Panama, and also to the Province of Colon, located in the Caribbean area of Panama.

No previous study about the distribution network of agricultural products has been previously conducted in Panama, hence the objective of the project is to develop an optimization model that helps understanding the behavior of the agricultural supply chain in Panamá, finding not only the minimum cost of satisfying supply and demand of agricultural products, but also to implement the minimum transportation cost of a vehicle assignment policy for the minimum allocation of products.

In order to better understand the behavior of the supply chain, several assumptions were made.

- In order to facilitate the initial understanding of the model, only one product will be selected.
- The selected produce is lettuce.
- Supplies and demands at different sources, transshipments and destinations will be considered weekly.

11th Latin American and Caribbean Conference for Engineering and Technology

- No inventories are allowed in intermediate points.
- Only three types of vehicles will be considered: pick-ups, trucks and trailers, as seen in figure 2.
- All costs, demands, supplies and availability of vehicles are known.
- No unloading and downloading times are considered.
- The unit load considered is the 40 lbs. crate of lettuce, as seen in figure 3.
- No returning of products.
- The cost is divided on two: the transportation cost, that considers production and loading costs, and the vehicle related cost that considers fuel, operation costs and depreciation.
- Production cost is constant and does not depend on the final destination. Thus, it is a fixed cost and has no influence on the model.



Figure 1: Agricultural Distribution Network



Figure 2: Types of vehicles

Figure 3 Unit load

3. LITERATURE REVIEW

Studying food distribution systems becomes an important point in supply chain management for several reasons. First of all, food scarcity becomes critical nowadays due to climate changes. Thus, cost of food and produces are increasing. On the other hand, people need food to be accessible and safe, in terms of availability, effects in health and costs, becoming a strategic issue for governments. For example, Pietro and Timpanaro (2012) affirm that the issue of agricultural logistics is the subject of great interest because it is considered strategic for the development of a country especially on the possible transport links between different areas of the country.

Boudahri, et al (2012) define the term agri-food supply chains (ASC) to describe the activities from production to distribution that bring agricultural or horticultural products from the farm to the table. ASC are formed by the farmers, distribution, processing, and marketing of agricultural products to the final consumers. In Panama, the interface between producers and supermarkets or municipal supply centers (final destination) is completely

monopolized by intermediaries (carriers) which increases the final product cost. All of these intermediates make up almost all the distribution networks for agricultural products in the internal food supply. This carriers transport the products of more than 60% of total producers and the remaining 40% is transported by private companies. In addition, there are losses of 40% of transported products. Therefore, these wastes in produce are transferred to the final customer (Orozco and Tuñón, 2012).

Moving agricultural products between different points in the country implies handling issues regarding perishability of products, long and tortuous supply chains marked by the presence of several operators and no alternate roads, the need to maintain a cold chain to guarantee the quality of the final product, consumption behavior and habits, and the role that health aspects and organoleptic quality play in purchasing decisions of consumers, among others (Estrada, 2007). According to Pietro and Timpanaro (2012), the cost the agricultural logistics varies between 20-30% of the cost of the product. This can be even higher depending on the type of chain involved, *e.g* the distance from origin and the type of transportation considered. Thus, it is important to view the transportation and logistics system as a whole since "the production, exchange, distribution and consumption of agricultural products constitute the organic chain of agriculture reproduction. Any deficiency of them will affect the development of agriculture (Tan, 2012, p. 106)".

Moreover, it is important the study of distribution networks in order to address the different issues existing between the diverse parties involved in the transportation and distribution systems of products. Daganzo (1992), for example, establishes the principle of distribution network application with the goal of uniting one origin with one destination, one origin to many destinations and many to many systems using transshipment centers and providing methods to solve it. On the other hand, Agra (2008) demonstrated that the costs associated with the transport of goods represent a large part of the final cost.

Several papers have been found in the literature concerning the modeling of the agri-food supply chain. Boudahri, et al (2012), for example, presented a document concerned with the planning of a real agri-food supply chain for chicken meat for the city of Tlemcen in Algeria. The agri-food supply chain network design is a critical planning problem for reducing the cost of the chain. More precisely the problem is to redesign the existing supply chain and to optimize the distribution planning. The authors applied the Allocation Problem Model in order to define points in the network with the objective of minimizing the total distance between customers and these sites, or to minimize the maximum distance.

Jones, et al (2001), on the other hand, consider a production-scheduling problem arising when there are random yields and demands as well as two sequential production periods before demand occurs. The paper presented a two-period model with random yield and random demand in which production can occur in either or both periods. The model is solved optimally as a sequential decision problem and it demonstrated that the two-period production strategy has substantial economic payoff for the seed industry.

Shu-quan and Ling (2010) focused the research in the multi-dimension and uncertainty of logistics performance evaluation for agricultural products distribution centers and the lack of evaluation methods, The authors proposed a hierarchy model of evaluation factors that combines fuzzy analytical hierarchy process (FAHP) with fuzzy comprehensive evaluation to generate quantitative comprehensive evaluation of logistics performance for agricultural products. They proved the rationality and application of this method through a practical case. Finally, Jang and Klein (2011), developed models for agricultural supply chains based on the stochastic aspects of risk and return on investment that small enterprises face, and suggest their uses and future considerations.

Related with the purpose of this paper, Mejia and Castro (2007) worked in the logistics optimization in a Colombian frozen and refrigerated food company. The authors developed a decision model based on linear programming to determine packing and distribution policies of frozen products. Zhang, et al (2011), on the other hand, focused on the research of a distribution model and vehicle routing optimization of fresh agricultural products. On the basic of detailed researching of agricultural products logistic characters, the paper establishes a vehicle optimization model suitable for transferring kinds of perishable agricultural products, to solve the severe

losing of fresh produce logistics with transportation distance. The model is solved by a genetic algorithm and the algorithm's effectiveness is verified using different examples.

4. MODEL DESCRIPTION AND SOLUTION

To develop the mathematical model, the Minimal Cost Network Flows (Bazaraa et al, 2005) approach was used, considering the different elements involved in the network. Thus, points as production centers, distribution points and final markets will be introduced, and a transshipment approach will be structured, and the optimal amount of lettuce through the network will be determined. In addition, a minimal flow problem consisting on modeling the optimal amount and types of vehicles used to deliver the lettuce will be included in the general model.

4.1 MODEL DESCRITPION

Consider a general network G = (V, A) where V is a vertex set representing either production centers, distribution centers of final markets, and A a set of directed arcs connecting different points in the set V. Every arch A is defined by the pair of indexes *i*, *j* indicating the origin and destination of such arch.

Let $x_{i,j}$ be the amount of products sent from point *i* to point *j*. In addition, consider $y^{(k)}_{i,j}$ the type of vehicle k used to transport products from point *i* to point *j*. Let $c_{i,j}$, the cost of moving one unit of product and and $b^{(k)}_{i,j}$ the cost of moving vehicle type *k* from point *i* to point *j*. Moreover, consider distribution or transshipment points *l* that define the transportation policy of the logistic system. The objective of the problem is to optimize the amount of products sent from the origins to destinations and the optimum amount and type of vehicles used to move the products, at a minimum cost.

Consider the following parameters:

Ζ	:	Total weekly cost of the transportation policy.
$N^{(k)}{}_{i}$:	Amount of vehicles type k available at point i.
$A^{(k)}$:	Capacity of vehicle type k in terms of unit loads.
S_i	:	Weekly supply of point i.
D_j	:	Weekly demand at point j.
W_l	:	Weekly capacity of the distribution or transshipment points.
т	:	Number of origins.
n	:	Number of destinations.
L	:	Number of distribution centers.
Κ	:	Vehicle types, in this case pick-ups, trucks and trailers.

The model is expressed bellow:

$$minZ = \sum_{i} \sum_{j} C_{ij} x_{ij} + \sum_{i} \sum_{j} \sum_{k} b_{ij}^{(k)} y_{ij}^{(k)}$$

$$\tag{1}$$

Subject to:

• Weekly capacity of the sources:

$$\sum_{t} x_{t,t} \le S_t \,\forall f \tag{2}$$

The first constraint requires that the different supply points send no more than the production available at each of them, thus the upper limit of the distribution policy is the maximum supply available at the different production points.

• Weekly demand of the destination points:

$$\sum_{j} x_{tj} \ge \mathbf{D}_{j} \,\forall t \tag{3}$$

11th Latin American and Caribbean Conference for Engineering and Technology

Cancun, Mexico

For every destination point, the amount sent by the sources must be at least the demand required by each destination point.

• No inventory in the transshipment points:

$$\sum_{t} x_{t,l} = \sum_{t} x_{lt} \ \forall l \tag{4}$$

Due to the perishability of the lettuce, no inventory will be allowed at the different origin, transshipment and destination points. Thus, any amount sent from the origins to the transshipment points has to be sent to the destination points.

• Weekly capacity of the distribution points:

$$\sum_{i} x_{ii} \le W_i \tag{5}$$

Each distribution or transshipment point has an specific capacity of storage that must be satisfied with every shipment of products from the production point.

• Weekly availability of vehicles:

$$\sum_{k} \sum_{j} y_{ij}^{(k)} \leq N_{i}^{(k)} \,\forall k, j \tag{6}$$

The amount of every type of vehicle used to transport lettuce at any supply point (considering also the transshipment points) must be less or equal to the available amount of vehicles at each of these points.

• Weekly transportation capacity of the vehicles at every distribution point:

$$\sum_{j} A^{(k)} y_{ij}^{(k)} - \sum_{j} x_{ij} \ge 0$$
(7)

At every distribution point, the capacity of all the available vehicles must be at least the amount ready to be sent to every destination point, thus vehicles are to be used only with this product.

• All variables are integer and bounded by their upper limits.

$$x_{ij}; y_{ij}^{(k)} \in I; \forall \begin{cases} i = 1, \dots, n\\ j = 1, \dots, n\\ l = 1, \dots, L\\ k = 1, \dots, K \end{cases}$$
(8)

4.2 MODEL SOLUTION METHOLOGY AND RESULTS

A feasible initial solution using Excel Solver was found. This approach was used to see the solvability of the model, and if the preliminary solutions had a plausible answer.

The solution shown in the following tables depict the optimal solution of the problem divided in two sections:

- The first section shows the amount of crates moved from the supply to demand points.
- The second section shows the amount of vehicles used to comply with the distribution program.

Table 1 shows the distribution policy for the lettuce. As seen, the total demand is satisfied using all the supplies from the different distribution points. This distribution policy takes into account the amount delivered to the intermediate points, Santiago and Mercado that are then delivered to the final consumption points.

From/To	David	Santiago	Chitré	Las Tablas	Aguadulce	Penonomé	Chorrera	Mercado	San Miguelito	Panamá Este	Colón	Total	Supply (S _i)
Boquete	0	770	0	0	0	0	0	5,500	0	0	0	6,270	6,500
Cerro Punta	2,000	1,980	0	0	0	0	0	3,200	0	0	0	7,180	8,000
Mercado	0	0	0	0	0	0	1,200	0	1,400	600	1,000	4,200	5,500
Santiago	0	0	750	200	250	350	0	0	0	0	0	1,550	3,200
Total	2,000	2,750	750	200	250	350	1,200	8,700	1,400	600	1,000	19,200	23,300
Demand (Dj)	2,000	2,750	750	200	250	350	1,200	8,700	1,400	600	1,000		

 Table 1: Crates Moved (x_{ij})

Tables 2 to 4 show the optimum amount of vehicles recommended to accomplish the distribution policy shown in table 1. As seen, the amount of vehicles used satisfies the availability of the corresponding vehicles: pick-ups, trucks and trailers. Further, the model recommends the use of large transport for longer routes rather than small vehicles, taking advantage of the low unitary cost of transportation in large vehicles.

It is important to recall that, since the model is limited to one product, it considers that the vehicles are dedicated only to transport one product, not to share space with other products.

From/To	David	Santiago	Chitré	Las Tablas	Aguadulce	Penonomé	Chorrera	Mercado	San Miguelito	Panamá Este	Colón	Total	Available Pickups (N _{ki})
Boquete	0	9	0	0	0	0	0	0	0	0	0	9	12
Cerro Punta	1	0	0	0	0	0	0	0	0	0	0	1	15
Mercado	0	0	0	0	0	0	7	0	0	6	0	13	45
Santiago	0	0	0	0	0	0	0	0	0	0	0	0	20
Total	1	9	0	0	0	0	7	0	0	6	0	23	

 Table 2: Pick-ups used

From/To	David	Santiago	Chitré	Las Tablas	Aguadulce	Penonomé	Chorrera	Mercado	San Miguelito	Panamá Este	Colón	Total	Available Trucks (N _{ki})
Boquete	0	2	0	0	0	0	0	6	0		0	8	8
Cerro Punta	0	0	0	0	0	0	0	9	0	0	0	9	9
Mercado	0	0	0	0	0	0	4	0	6	2	0	12	12
Santiago	0	0	3	1	1	2	0	0	0	0	0	7	10
Total	0	2	3	1	1	2	4	15	6	2	0	36	

Table 3: Trucks used

Table 4: Trailers used

From/To	David	Santiago	Chitré	Las Tablas	Aguadulce	Penonomé	Chorrera	Mercado	San Miguelito	Panamá Este	Colón	Total	Available Trailers (N _{ki})
Boquete	0	0	0	0	0	0		4	0	0	0	4	4
Cerro Punta	2	2	0	0	0	0	0	1	0	0	0	5	5
Mercado	0	0	0	0	0	0	0	0	0	0	1	1	2
Santiago	0	0	0	0	0	0	0	0	0	0	0	0	2
Total	2	2	0	0	0	0	0	5	0	0	1	10	

11th Latin American and Caribbean Conference for Engineering and Technology

Finally, table 5 shows a summary of the optimal solution for the problem. Minimum cost for delivering 19,200 crates per week is \$80,790. The distribution program uses 23 pick-ups, 36 trucks and 10 trailers at a total weekly transportation cost of \$6,190.

Objective Function	\$ 80,790
For delivering 19,2 per week	200 Lettuce Crates
Using	At a total weekly cost of:
23 Pick-ups	\$ 415.00
36 Trucks	\$ 1,825.00
10 Trailers	\$ 3,950.00

Table 5:	Optimal	Solution	Summary

*Solved using Solver with Simplex LP

5. CONCLUSIONS AND FUTURE WORK

The model provided a solution with a distribution policy consisting on both, amounts to be moved from origins to destinations and vehicles to be used. All these variables are tied to costs, such that the result provides, in addition, the minimum cost of the policy.

At his stage of the project several important conclusions can be drawn from this paper. First of all, the lack of information on costs, routing, demands and supplies makes really difficult to gather valid information to formulate and evaluate de model. Further, there are no congruence between data from the producers and official institutions. Thus, it is very difficult to validate the results of the model. Finally, it is necessary for the different organizations involved in the agro-food supply chain, to work in a more united manner since it is important to maintain the supply chain efficient and effective for all, producers, suppliers, and final consumers.

Since this is the first stage of a more ambitious project, work is still pending. For example, the model has to be feed with more current data, and more variables and constrains need to be tested in the model. For instance, to see what might happen if time and more frequencies are added.

Furthermore, it is necessary to add more products, thus the problem becomes a multicommodity flows problem (Bazaraa, et al, 2005) which increases the complexity of the problem adding a number of variables and constraints proportional to the amount of products. In addition, it is necessary to include an additional objective since it is important to maximize the value of the load in each transport, because the load in each transport has to be the optimal combination of products. Henceforth, the problem becomes a multicriteria, multicommodity minimum flow problem with equipment assignment.

6. AUTHORIZATION AND DISCLAIMER

"Authors authorize LACCEI to publish the papers in the conference proceedings. Neither LACCEI nor the editors are responsible either for the content or for the implications of what is expressed in the paper."

AKNOWLEDGEMENT

The project is supported by a grant from the National Secretary of Science, Technology and Innovation of Panama. In addition it is supported with facilities and infrastructure by the Technological University of Panama and The International Maritime University of Panama. Finally, it is important to acknowledge the support of Dr. Mario Serrato from the Tec de Monterrey in reviewing of the model.

REFERENCES

- Boudahri, et al. (2012). "Application of a Capacitated Centered Clustering Problem for Design of Agri-food Supply Chain Network". *IJCSI International Journal of Computer Science Issues*, Vol. 9, No. 4, pp.1694-1814.
- Orozco, A., and Tuñon, G. (2012). "Designing a Logistic Platform through the Optimization of the Distribution Networks for the Agricultural Sector". *Proceedings of the 5th. International Conference on Maritime Transportation*, Martinez de Oses, F. X., and Castells, M., editors. Universitat Politectnica de Catalunya, pp. 95-109,
- Pietro, P., and Timpanaro, G. (2012). "Ethics, Sustainability and Logistics in Agricultural and Agri-food Economics Research". *Italian Journal of Agronomy*, Vol.7, No. 33, pp. 237 246.
- Tan, D. (2012). "Developing Agricultural Products Logistics in China from the Perspective of Green Supply Chain". *International Journal of Business and Management*, Vol.7, No. 21, 106-112.
- Daganzo, C. (1992). Logistics Systems Analysis. 1st. Edition, Springer-Verlag, USA.
- Agra D., (2008), "Localización de centros de intercambio modal y plataformas logísticas". Master's thesis, Universitat Politecnica de Catalunya.
- Estrada, M. (2007). "Análisis de estrategias eficientes en la logística de distribución de paquetería". Doctoral Dissertation, Universitat Politecnica de Catalunya.
- Jones, P., et al. (2001). "Matching Supply and Demand: The Value of a Second Chance in Producing Hybrid Seed Corn". *Manufacturing and Service Operations Management*, Vol. 3, No. 2, pp. 122-137.
- Shu-quan, L., and Ling, L. (2010). "Comprehensive Evaluation of Logistics Performance for Agricultural Products Distribution Center." *Proceedings of the 2010 2nd International Conference on E-Business and Information Systems Security*, May 4-7, Wuhan, China.
- Jan, W., and Klein, K. (2011). "Supply Chain Models for Small Agricultural Enterprises". Annals of Operations Research, Vol. 190, No. 1, pp. 359-374.
- Mejía, G., and Castro, E. (2007) "Logistics Optimization in a Colombian Frozen and Refrigerated Foods Company". Revista de Ingeniería. Universidad de los Andes. Bogotá, Colombia, No, 26, pp. 47-54.
- Zhang, S., et al. (2011). "Research of Fresh Agricultural Products Logistics Vehicle Optimization". International Journal of Intelligent Information Processing, Vol.2, No. 2, 45-58.
- Bazaraa, M., et al. (2005). *Linear Programming and Network Flows*. 3rd Edition, Wiley Interscience, New Jersey, USA.

AUTHORIZATION AND DISCLAIMER

Authors authorize LACCEI to publish the paper in the conference proceedings. Neither LACCEI nor the editors are responsible either for the content or for the implications of what is expressed in the paper.